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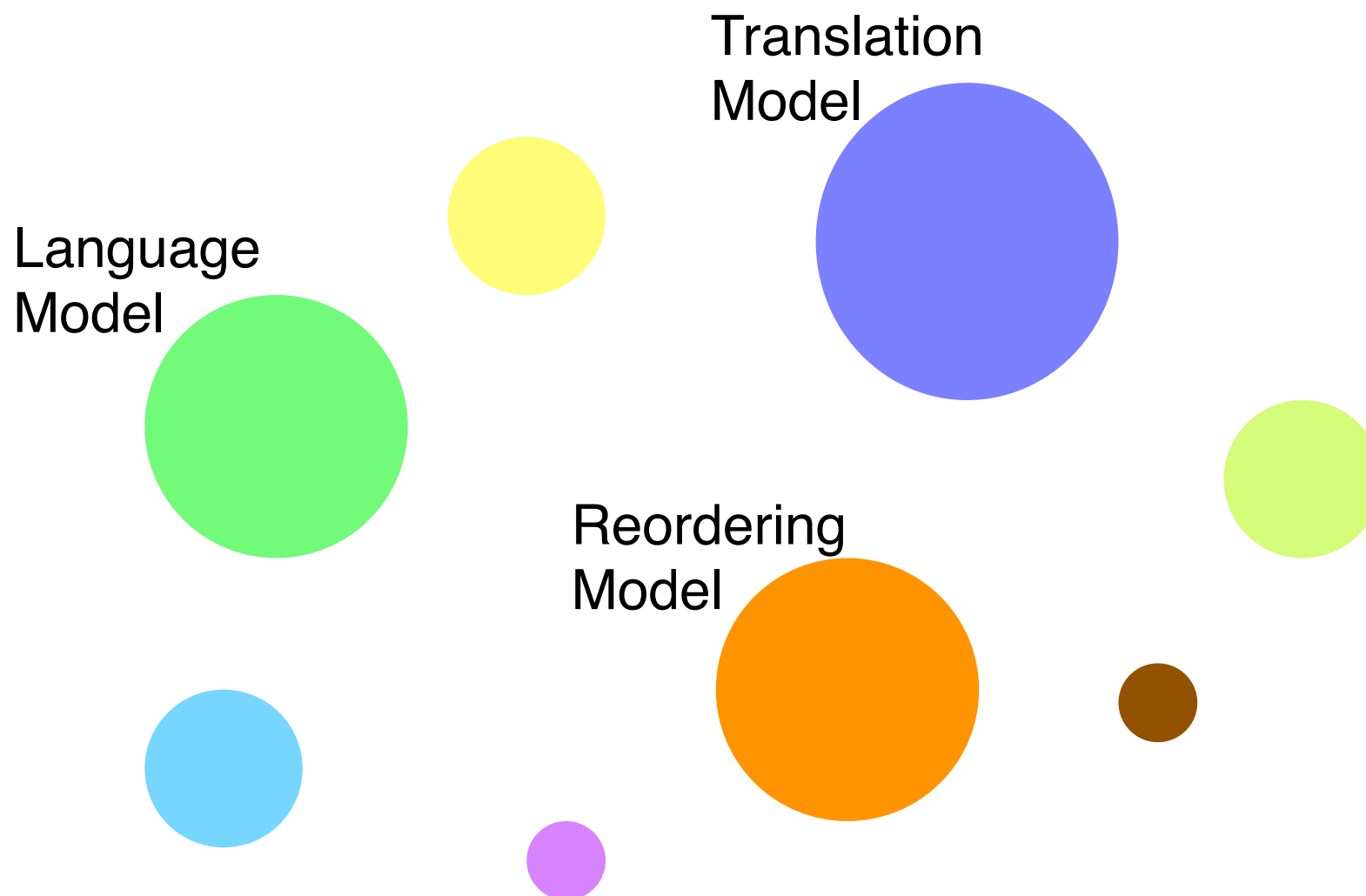
# Sparse Feature Learning

Philipp Koehn

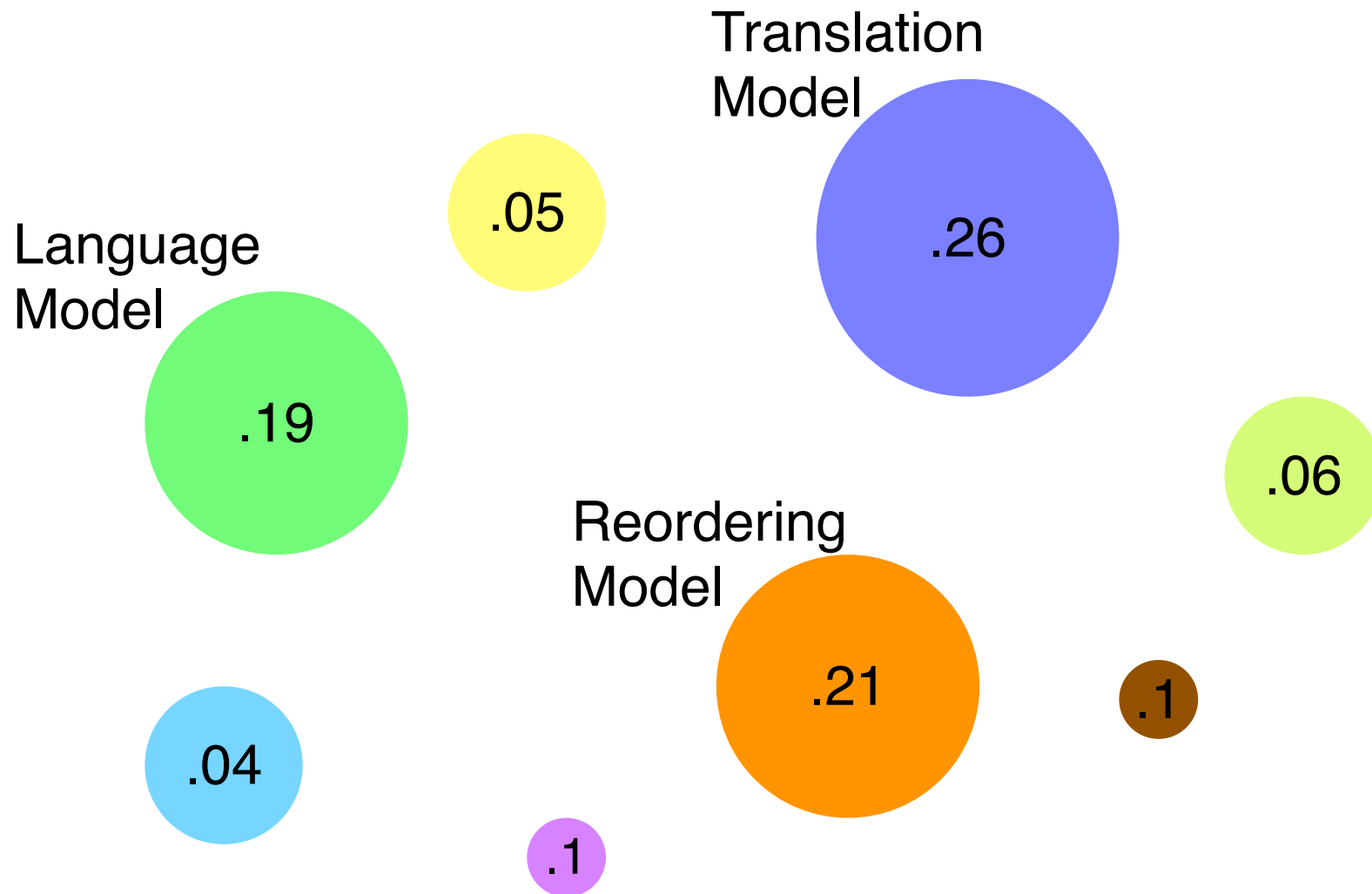
3 March 2015



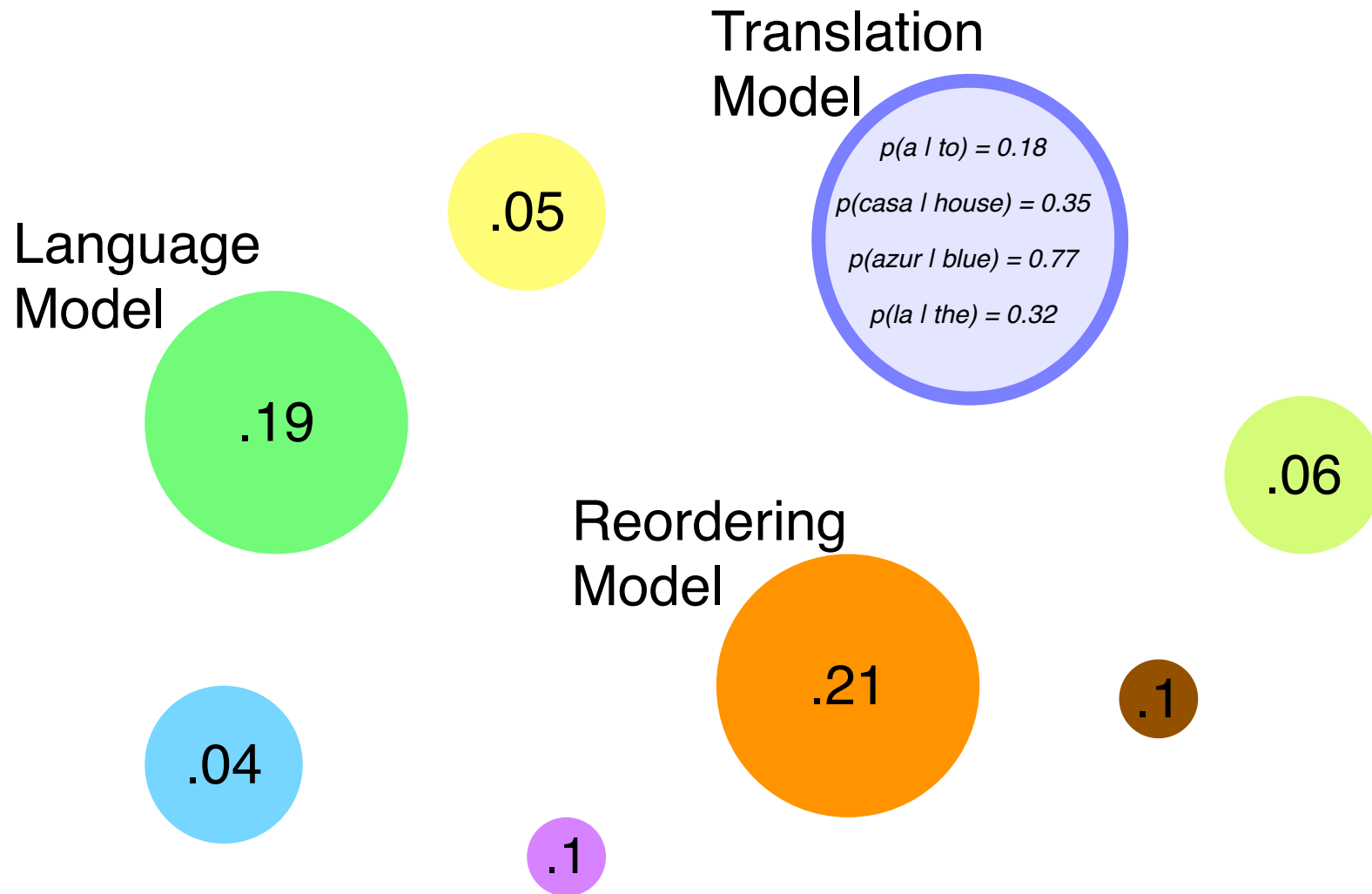
# Multiple Component Models



# Component Weights



# Even More Numbers Inside

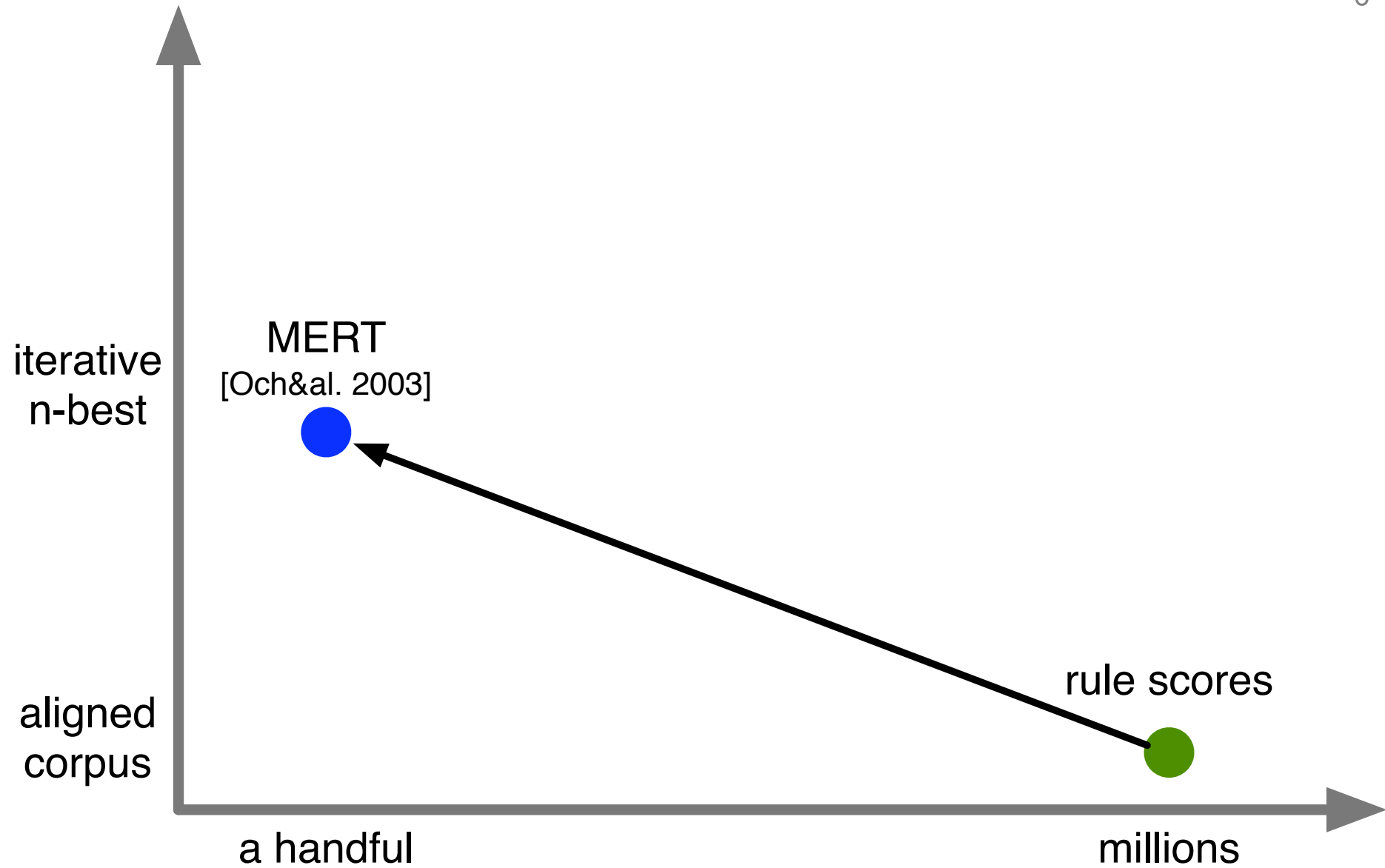


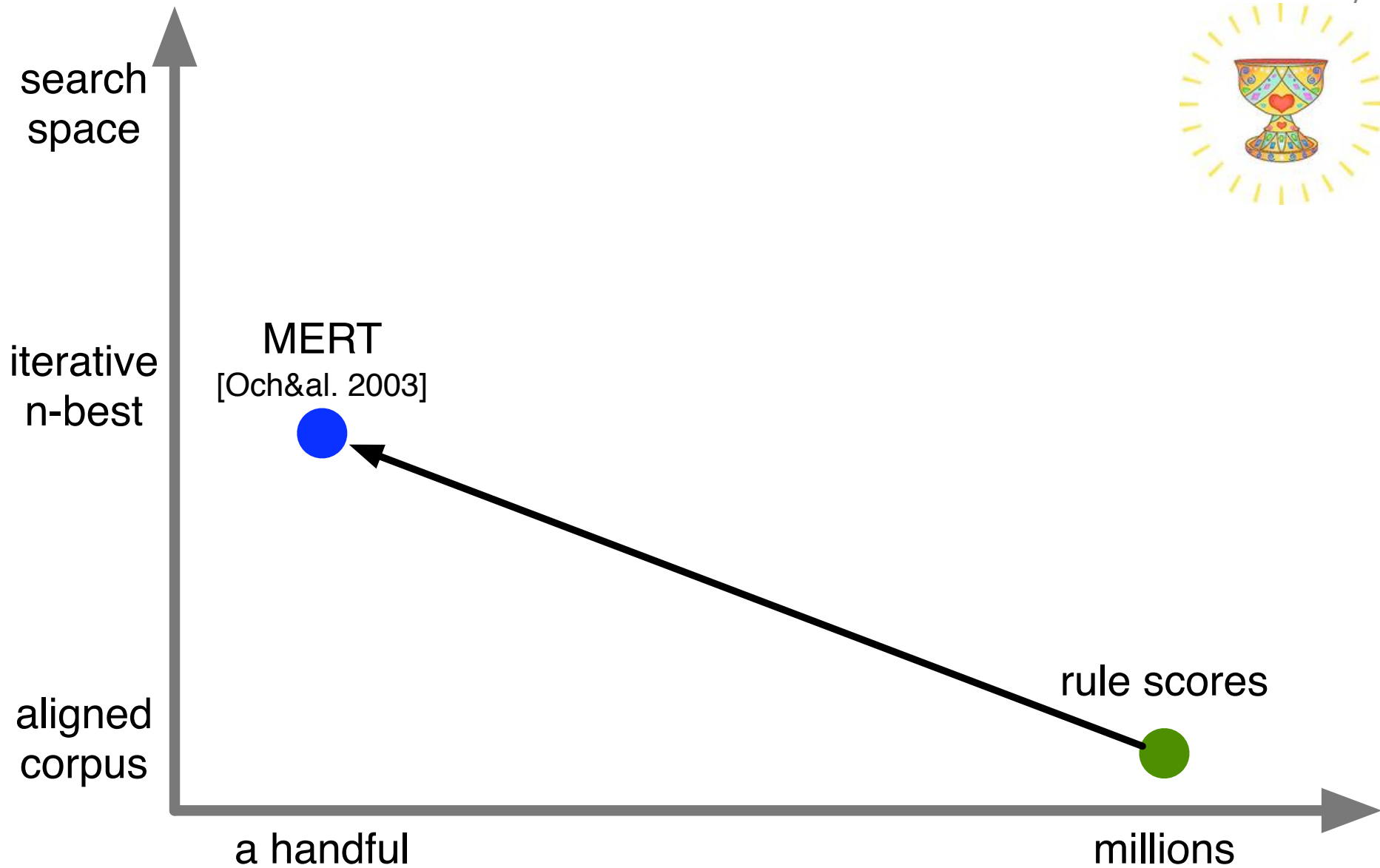
# Grand Vision



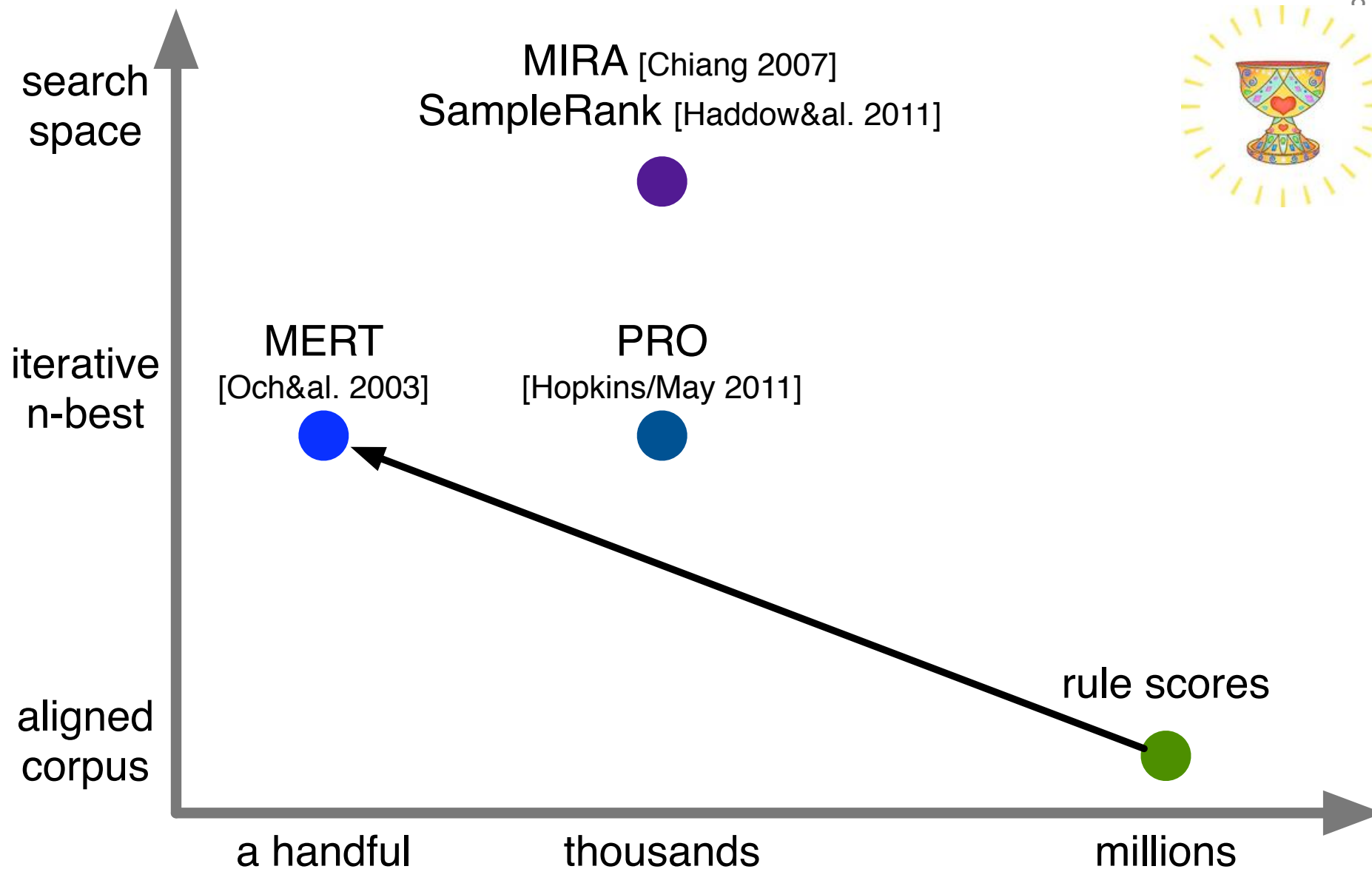
- There are millions of parameters
  - each phrase translation score
  - each language model n-gram
  - etc.
- Can we train them all discriminatively?
- This implies optimization over the entire training corpus

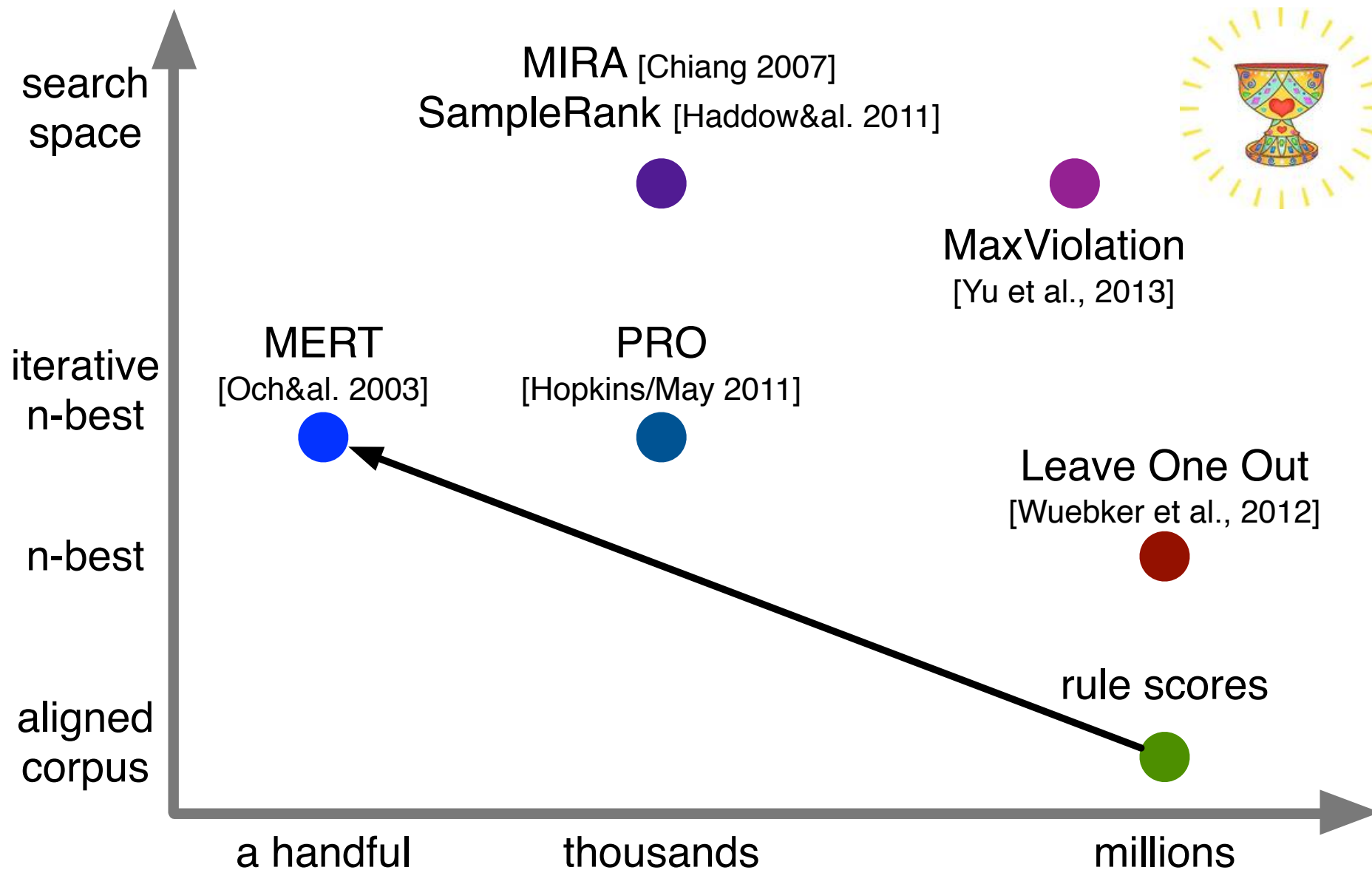












# Strategy and Core Problems



- Process each sentence pair in the training corpus
- Optimize parameters towards producing the reference translation
- Reference translation may not be producible by model
  - optimize towards most similar translation
  - or, only process sentence pair partially
- Avoid overfitting
- Large corpora require efficient learning methods

# Sentence Level vs. Corpus Level Error Metric<sup>11</sup>



- Optimizing BLEU requires optimizing over the entire training corpus

$$\text{BLEU}(\{\mathbf{e}_i^{\text{best}} = \text{argmax}_{\mathbf{e}_i} \sum_j h_j(\mathbf{e}_i, \mathbf{f}_i) \lambda_i\}, \{\mathbf{e}_i^{\text{ref}}\})$$

- Life would be easier, if we could sum over sentence level scores

$$\sum_i \text{BLEU}'(\text{argmax}_{\mathbf{e}_i} \sum_j h_j(\mathbf{e}_i, \mathbf{f}_i) \lambda_i, \mathbf{e}_i^{\text{ref}})$$

- For instance, BLEU+1



# features

# Core Rule Properties

- Frequency of phrase (binned)
- Length of phrase
  - number of source words
  - number of target words
  - number of source and target words
- Unaligned / added (content) words in phrase pair
- Reordering within phrase pair

- $\text{lex}(e)$  fires when an output word  $e$  is generated
- $\text{lex}(f, e)$  fires when an output word  $e$  is generated aligned to a input word  $f$
- $\text{lex}(\text{NULL}, e)$  fires when an output word  $e$  is generated unaligned
- $\text{lex}(f, \text{NULL})$  fires when an input word  $e$  is dropped
- Could also be defined on part of speech tags or word classes

# Lexicalized Reordering Features

- Replacement of lexicalized reordering model
- Features differ by
  - lexicalized by first or last word of phrase (source or target)
  - word representation replaced by word class
  - orientation type



- Indicator feature that the rule occurs in one specific domain
- Probability that the rule belongs to one specific domain
- Domain-specific lexical translation probabilities

- If we have syntactic parse trees, many more features
  - number of nodes of a particular kind
  - matching of source and target constituents
  - reordering within syntactic constituents
- Parse trees are a by-product of syntax-based models
- More on that in future lectures

# Every Number in Model

- Phrase pair indicator feature
- Target n-gram feature
- Phrase pair orientation feature

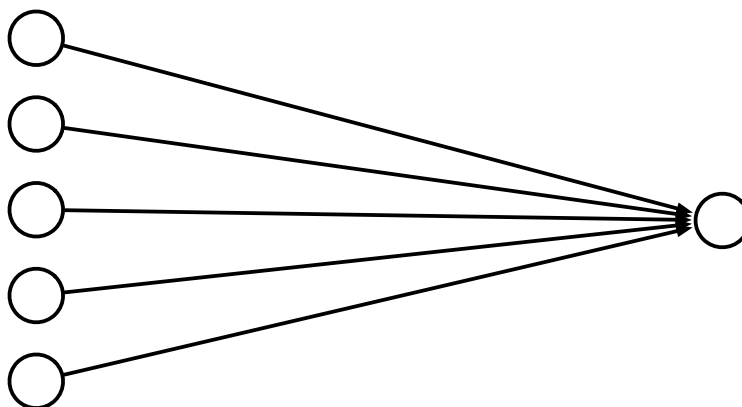
# perceptron algorithm

# Optimizing Linear Model

- We consider each sentence pair  $(\mathbf{e}_i, \mathbf{f}_i)$  and its alignment  $\mathbf{a}_i$
- To simplify notation, we define derivation  $\mathbf{d}_i = (\mathbf{e}_i, \mathbf{f}_i, \mathbf{a}_i)$
- Model score is weighted linear combination of feature values  $h_j$  and weights  $\lambda_j$

$$\text{score}(\lambda, \mathbf{d}_i) = \sum_j \lambda_j h_j(\mathbf{d}_i)$$

- Such models are also known as single layer perceptrons



# Reference and Model Best

- Besides the reference derivation  $\mathbf{d}_i^{\text{ref}}$  for sentence pair  $i$  and its score

$$\text{score}(\lambda, \mathbf{d}_i^{\text{ref}}) = \sum_j \lambda_j h_j(\mathbf{d}_i^{\text{ref}})$$

- We also have the model best translation

$$\mathbf{d}_i^{\text{best}} = \text{argmax}_{\mathbf{d}} \text{score}(\lambda, \mathbf{d}_i) = \text{argmax}_{\mathbf{d}} \sum_j \lambda_j h_j(\mathbf{d}_i)$$

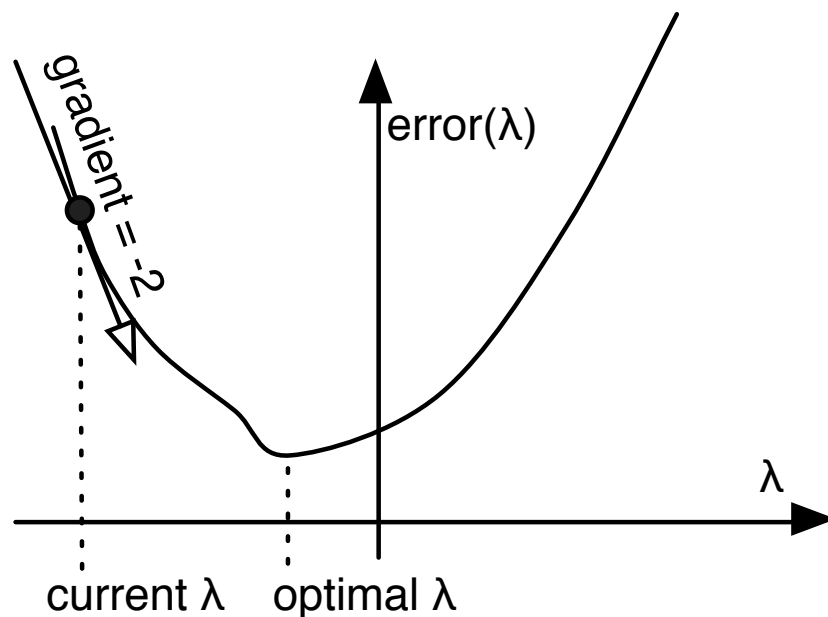
- ... and its model score

$$\text{score}(\lambda, \mathbf{d}_i^{\text{best}}) = \sum_j \lambda_j h_j(\mathbf{d}_i^{\text{best}})$$

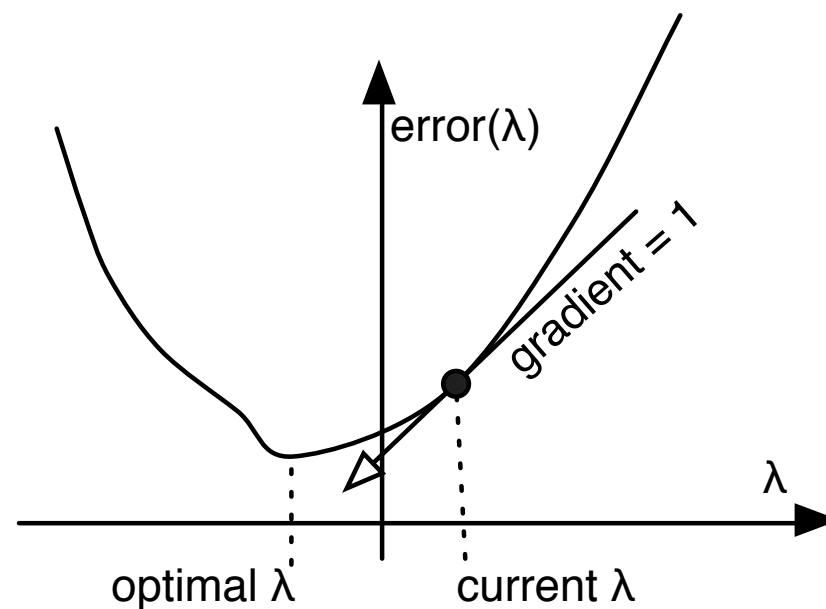
- We can view the error in our model as a function of its parameters  $\lambda$

$$\text{error}(\lambda, \mathbf{d}_i^{\text{best}}, \mathbf{d}_i^{\text{ref}}) = \text{score}(\lambda, \mathbf{d}_i^{\text{best}}) - \text{score}(\lambda, \mathbf{d}_i^{\text{ref}})$$

# Follow the Direction of Gradient



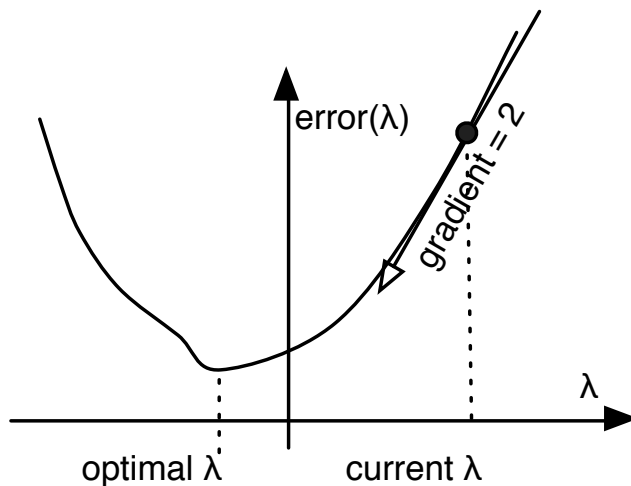
gradient negative  
 $\Rightarrow$  we need to move right



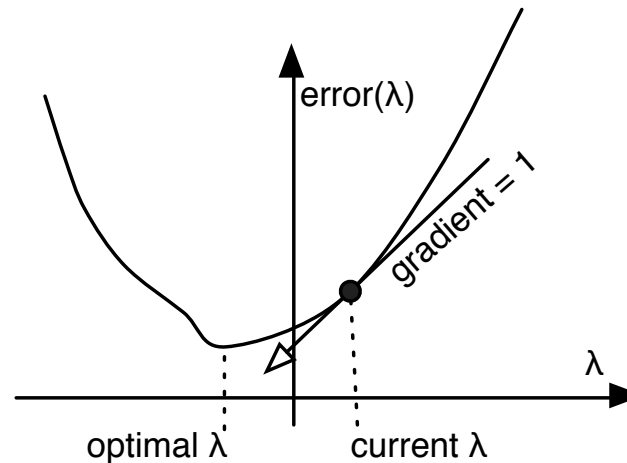
gradient positive  
 $\Rightarrow$  we need to move left

- Assume that we can compute the gradient  $\frac{d}{d\lambda}\text{error}(\lambda)$  at any point
- If the error curve is convex, gradient points in the direction the optimum

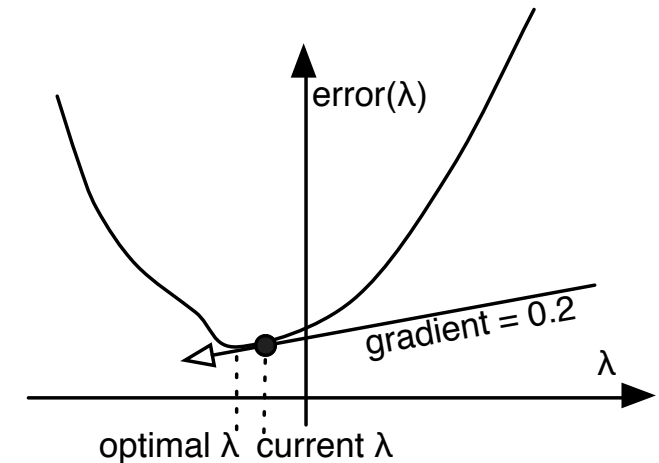
# Move Relative to Steepness



gradient high (steep)  
 $\Rightarrow$  move a lot



gradient medium  
 $\Rightarrow$  move some



gradient low (flat)  
 $\Rightarrow$  move little

- If the error curve is convex, size of gradient indicates speed of change
- Model update  $\Delta\lambda = -\frac{d}{d\lambda}\text{error}(\lambda)$



# Stochastic Gradient Descent

- We want to minimize the error

$$\text{error}(\lambda, \mathbf{d}_i^{\text{best}}, \mathbf{d}_i^{\text{ref}}) = \text{score}(\lambda, \mathbf{d}_i^{\text{best}}) - \text{score}(\lambda, \mathbf{d}_i^{\text{ref}})$$

- In stochastic gradient descent, we follow direction of gradient

$$\frac{d}{d \lambda} \text{error}(\lambda, \mathbf{d}_i^{\text{best}}, \mathbf{d}_i^{\text{ref}})$$

- For each  $\lambda_j$ , we compute the gradient pointwise

$$\frac{d}{d \lambda_j} \text{error}(\lambda_j, \mathbf{d}_i^{\text{best}}, \mathbf{d}_i^{\text{ref}}) = \frac{d}{d \lambda_j} \text{score}(\lambda, \mathbf{d}_i^{\text{best}}) - \text{score}(\lambda, \mathbf{d}_i^{\text{ref}})$$

- Gradient with respect to  $\lambda_j$

$$\frac{d}{d \lambda_j} \text{error}(\lambda_j, \mathbf{d}_i^{\text{best}}, \mathbf{d}_i^{\text{ref}}) = \frac{d}{d \lambda_j} \sum_{j'} \lambda_{j'} h_{j'}(\mathbf{d}_i^{\text{best}}) - \sum_{j'} \lambda_{j'} h_{j'}(\mathbf{d}_i^{\text{ref}})$$

- For  $\lambda'_{j'} \neq \lambda_j$ , the terms  $\lambda_{j'} h_{j'}(\mathbf{d}_i)$  are constant, so they disappear

$$\frac{d}{d \lambda_j} \text{error}(\lambda_j, \mathbf{d}_i^{\text{best}}, \mathbf{d}_i^{\text{ref}}) = \frac{d}{d \lambda_j} \lambda_j h_j(\mathbf{d}_i^{\text{best}}) - \lambda_j h_j(\mathbf{d}_i^{\text{ref}})$$

- The derivative of a linear function is its factor

$$\frac{d}{d \lambda_j} \text{error}(\lambda_j, \mathbf{d}_i^{\text{best}}, \mathbf{d}_i^{\text{ref}}) = h_j(\mathbf{d}_i^{\text{best}}) - h_j(\mathbf{d}_i^{\text{ref}})$$

$\Rightarrow$  Our model update is  $\lambda_j^{\text{new}} = \lambda_j - (h_j(\mathbf{d}_i^{\text{best}}) - h_j(\mathbf{d}_i^{\text{ref}}))$

- Feature values in model best translation
- Feature values in reference translation
- Intuition:
  - promote features whose value is bigger in reference
  - demote features whose value is bigger in model best

**Input:** set of sentence pairs ( $\mathbf{e}, \mathbf{f}$ ), set of features

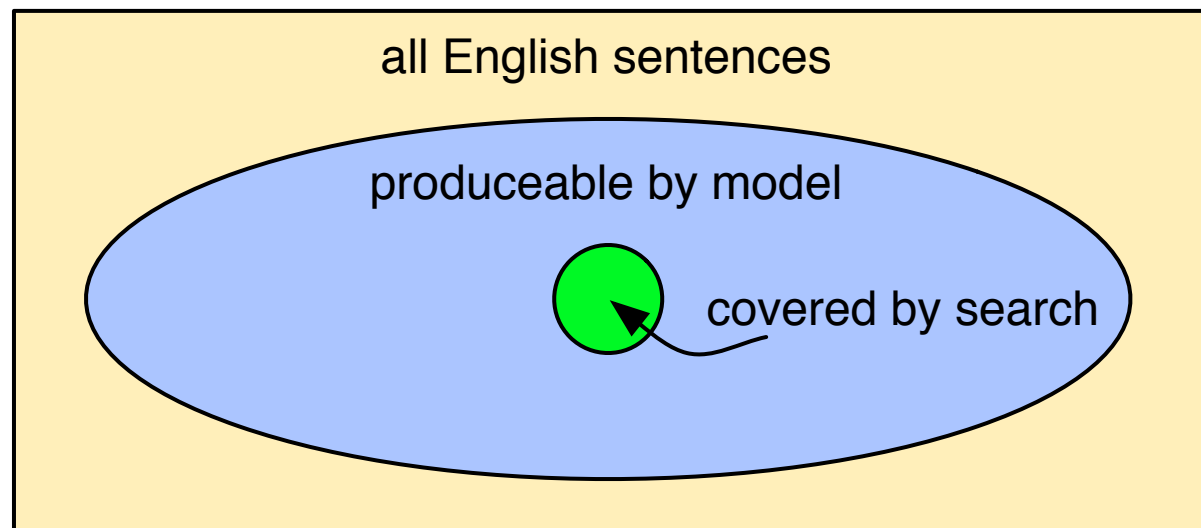
**Output:** set of weights  $\lambda$  for each feature

```
1:  $\lambda_i = 0$  for all  $i$ 
2: while not converged do
3:   for all foreign sentences  $\mathbf{f}$  do
4:      $\mathbf{d}_{\text{best}} =$  best derivation according to model
5:      $\mathbf{d}_{\text{ref}} =$  reference derivation
6:     if  $\mathbf{d}_{\text{best}} \neq \mathbf{d}_{\text{ref}}$  then
7:       for all features  $h_i$  do
8:          $\lambda_i += h_i(\mathbf{d}_{\text{ref}}) - h_i(\mathbf{d}_{\text{best}})$ 
9:       end for
10:    end if
11:  end for
12: end while
```

# generating the reference

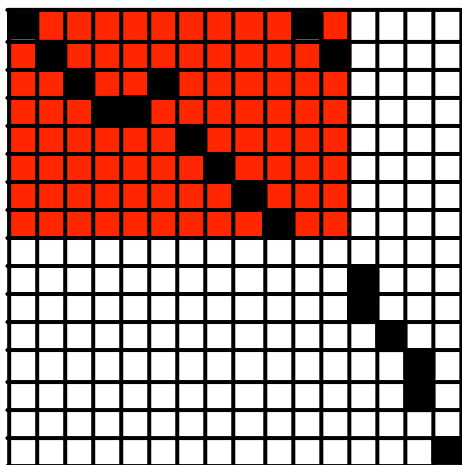
# Failure to Generate Reference

- Reference translation may be anywhere in this box

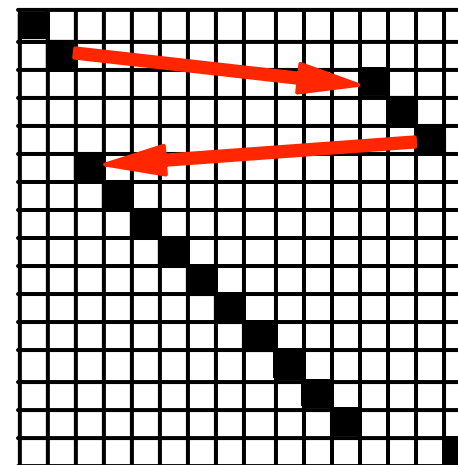


- If producible by model  $\rightarrow$  we can compute feature scores
- If not  $\rightarrow$  we can not

- Reference translation in tuning set not literal
- Failure even if phrase pairs are extracted from same sentence pair
- Examples



alignment points too distant  
→ phrase pair too big to extract



required reordering distance too large  
→ exceeds distortion limit of decoder

- BLEU+1
  - add one free n-gram count to statistics → avoids BLEU score of 0
  - however: wrong balance between 1-4 grams, too drastic brevity penalty
- BLEU impact
  - leave all other sentence translations fixed
  - collect n-gram matches and totals from them
  - add n-gram matches and total from current candidate
  - consider impact on overall BLEU score
- Incremental BLEU impact
  - maintain decaying statistics for n-gram matches, total n-grams

$$\text{count}_t = \frac{9}{10} \text{count}_{t-1} + \text{current-count}_t$$



# Problems with Max-BLEU Training

- Consider the following Arabic sentence (written left-to-right in Buckwalter romanization) with English glosses:

sd            qTEp   mn   AlkEk   AlmmlH   "   brytzl   "   Hlqh   .  
blocked   piece   of   biscuit   salted   "   pretzel   "   his-throat

- Very literal translation might be

A piece of a salted biscuit, a "pretzel," blocked his throat.

- But reference translation is

A pretzel, a salted biscuit, became lodged in his throat.

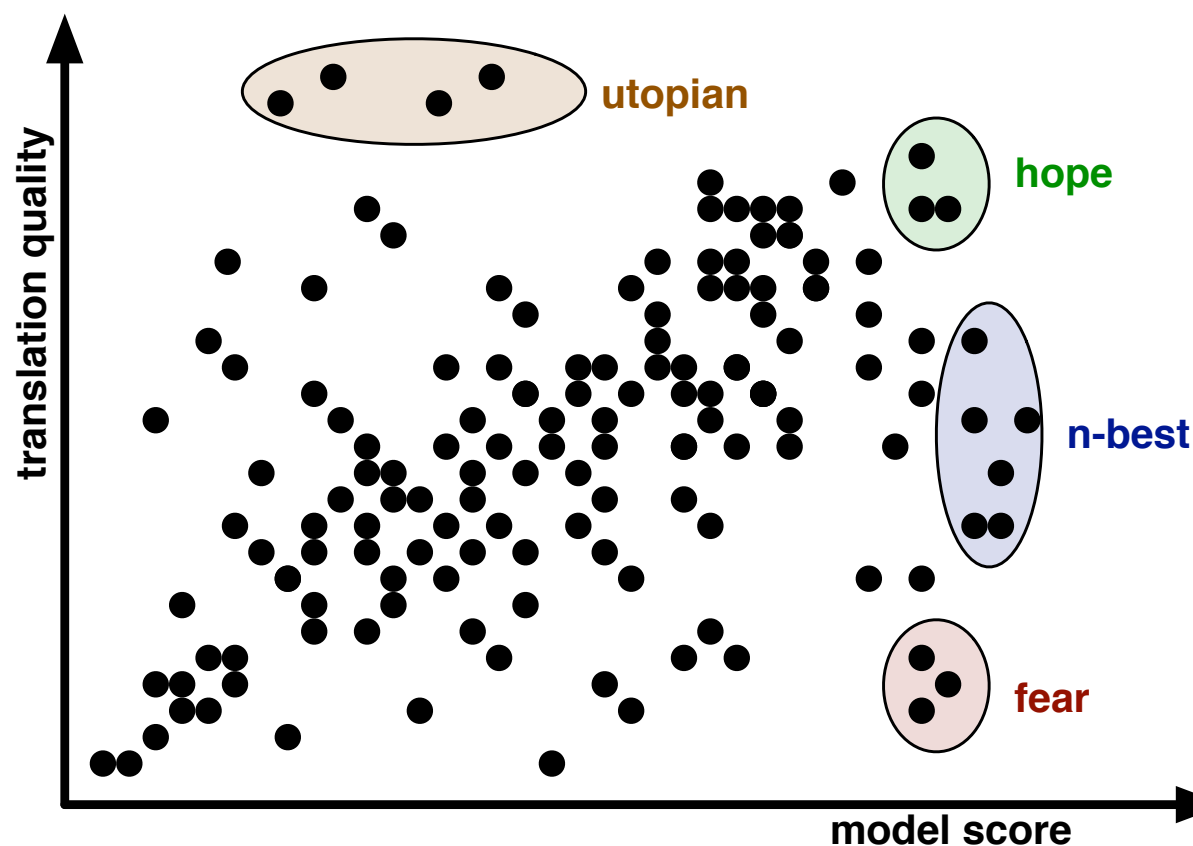
- Reference accurate, but major transformations
- Trying to approximate reference translation may lead to bad rules

note: example from Chiang (2012)

mira

# Hope and Fear

- Bad: optimize towards **utopian**, away from **n-best**
- Good: optimize towards **hope**, away from **fear**



# Hope and Fear Translations

- Hope translation

$$\mathbf{d}^{\text{hope}} = \operatorname{argmax}_{\mathbf{d}} \operatorname{BLEU}(\mathbf{d}) + \operatorname{score}(\mathbf{d})$$

- Finding the fear translation

- Metric difference (should be big)

$$\Delta \operatorname{BLEU}(\mathbf{d}^{\text{hope}}, \mathbf{d}) = \operatorname{BLEU}(\mathbf{d}^{\text{hope}}) - \operatorname{BLEU}(\mathbf{d})$$

- Score difference (should be small or negative)

$$\Delta \operatorname{score}(\lambda, \mathbf{d}^{\text{hope}}, \mathbf{d}) = \operatorname{score}(\lambda, \mathbf{d}^{\text{hope}}) - \operatorname{score}(\lambda, \mathbf{d})$$

- Margin

$$v(\lambda, \mathbf{d}^{\text{hope}}, \mathbf{d}) = \Delta \operatorname{BLEU}(\mathbf{d}^{\text{hope}}, \mathbf{d}) - \Delta \operatorname{score}(\lambda, \mathbf{d}^{\text{hope}}, \mathbf{d})$$

- Fear translation

$$\mathbf{d}^{\text{fear}} = \operatorname{argmax}_{\mathbf{d}} v(\lambda, \mathbf{d}^{\text{hope}}, \mathbf{d})$$

# Margin Infused Relaxed Algorithm (MIRA) 36



- Stochastic gradient descent update with learning weight  $\delta_i$

$$\lambda_j^{\text{new}} = \lambda_j - \delta_i \left( h_j(\mathbf{d}_i^{\text{fear}}) - h_j(\mathbf{d}_i^{\text{hope}}) \right)$$

- Updates should depend on margin

$$\delta_i = \min \left( C, \frac{\Delta_{\text{BLEU}}(\mathbf{d}_i^{\text{hope}}, \mathbf{d}_i^{\text{fear}}) - \Delta_{\text{score}}(\mathbf{d}_i^{\text{hope}}, \mathbf{d}_i^{\text{fear}})}{\|\Delta h\|^2} \right)$$

- The math behind this is a bit complicated

# Different Learning Rates for Features

- For some features, we have a lot of evidence (coarse features)
- Others occur only rarely (sparse features)
- After a while, we do not want to change coarse features too much

⇒ Adaptive Regularization of Weights (AROW)

- record confidence in weights over time
- include this in the learning rate for each feature

- Training is computationally expensive

⇒ Break up training data into batches

- After processing all the batches, average the weights
- Not only a speed-up, also seems to improve quality
- Allows parallel processing, but requires inter-process communication

- Generating hope and fear translations is expensive
  - Sample good/bad by random walk through alignment space
    - use operations as in Gibbs samples
    - vary one translation option choice
    - vary one reordering decision
    - vary one phrase segmentation decision
    - adopt new translation based on relative score
  - Compare current translation against its neighbors
- apply MIRA update if more costly translation has higher BLEU



- MIRA requires translation of each sentence on demand
  - repeated decoding needed
  - computationally very expensive
- Batch MIRA
  - n-best list or search graph (lattice)
  - straightforward parallelization
  - does not seem to harm performance



pro

# Scored N-Best List

- Reference translation: he does not go home
- N-best list

Translation	Feature values						BLEU+1
it is not under house	-32.22	-9.93	-19.00	-5.08	-8.22	-5	27.3%
he is not under house	-34.50	-7.40	-16.33	-5.01	-8.15	-5	30.2%
it is not a home	-28.49	-12.74	-19.29	-3.74	-8.42	-5	30.2%
it is not to go home	-32.53	-10.34	-20.87	-4.38	-13.11	-6	31.2%
it is not for house	-31.75	-17.25	-20.43	-4.90	-6.90	-5	27.3%
he is not to go home	-35.79	-10.95	-18.20	-4.85	-13.04	-6	31.2%
he does not home	-32.64	-11.84	-16.98	-3.67	-8.76	-4	36.2%
it is not packing	-32.26	-10.63	-17.65	-5.08	-9.89	-4	21.8%
he is not packing	-34.55	-8.10	-14.98	-5.01	-9.82	-4	24.2%
he is not for home	-36.70	-13.52	-17.09	-6.22	-7.82	-5	32.5%

- Higher quality translation (BLEU+1) should rank higher

# Pick 2 Translations at Random

- Reference translation: he does not go home
- N-best list

Translation	Feature values						BLEU+1
it is not under house	-32.22	-9.93	-19.00	-5.08	-8.22	-5	27.3%
he is not under house	-34.50	-7.40	-16.33	-5.01	-8.15	-5	30.2%
it is not a home	-28.49	-12.74	-19.29	-3.74	-8.42	-5	30.2%
it is not to go home	-32.53	-10.34	-20.87	-4.38	-13.11	-6	31.2%
<b>it is not for house</b>	-31.75	-17.25	-20.43	-4.90	-6.90	-5	<b>27.3%</b>
he is not to go home	-35.79	-10.95	-18.20	-4.85	-13.04	-6	31.2%
he does not home	-32.64	-11.84	-16.98	-3.67	-8.76	-4	36.2%
it is not packing	-32.26	-10.63	-17.65	-5.08	-9.89	-4	21.8%
he is not packing	-34.55	-8.10	-14.98	-5.01	-9.82	-4	24.2%
<b>he is not for home</b>	-36.70	-13.52	-17.09	-6.22	-7.82	-5	<b>32.5%</b>

- Higher quality translation (BLEU+1) should rank higher

# One is Better than the Other

- Reference translation: he does not go home
- N-best list

Translation	Feature values						BLEU+1
it is not under house	-32.22	-9.93	-19.00	-5.08	-8.22	-5	27.3%
he is not under house	-34.50	-7.40	-16.33	-5.01	-8.15	-5	30.2%
it is not a home	-28.49	-12.74	-19.29	-3.74	-8.42	-5	30.2%
it is not to go home	-32.53	-10.34	-20.87	-4.38	-13.11	-6	31.2%
<b>it is not for house</b>	<b>-31.75</b>	<b>-17.25</b>	<b>-20.43</b>	<b>-4.90</b>	<b>-6.90</b>	<b>-5</b>	<b>27.3%</b>
he is not to go home	-35.79	-10.95	-18.20	-4.85	-13.04	-6	31.2%
he does not home	-32.64	-11.84	-16.98	-3.67	-8.76	-4	36.2%
it is not packing	-32.26	-10.63	-17.65	-5.08	-9.89	-4	21.8%
he is not packing	-34.55	-8.10	-14.98	-5.01	-9.82	-4	24.2%
<b>he is not for home</b>	<b>-36.70</b>	<b>-13.52</b>	<b>-17.09</b>	<b>-6.22</b>	<b>-7.82</b>	<b>-5</b>	<b>32.5%</b>

- Higher quality translation (BLEU+1) should rank higher

# Learn from the Pairwise Sample

- Pairwise sample

- $\vec{\text{bad}} = (-31.75, -17.25, -20.43, -4.90, -6.90, -5)$
- $\vec{\text{good}} = (-36.70, -13.52, -17.09, -6.22, -7.82, -5)$

- Learn a classifier

- $\vec{\text{bad}} - \vec{\text{good}} \rightarrow \text{☹}$
- $\vec{\text{good}} - \vec{\text{bad}} \rightarrow \text{☺}$

- Use off the shelf maximum entropy classifier to learn weights for each feature  
e.g., MegaM (<http://www.umi.acs.umd.edu/~hal/megam/>)

- Collect samples for each sentence pair in tuning set
- For each sentence, sample 1000-best list for 50 pairwise samples
- Reject samples if difference in BLEU+1 score is too small ( $\leq 0.05$ )
- Iterate process
  1. set default weights
  2. generate n-best list
  3. build classifier
  4. adopt classifier weights
  5. go to 2, unless converged

# leave one out



# Leave One Out Training

- Train initial baseline model
- Force translate the training data:  
require decoder to match the reference translation
- Collect statistics over translation rules used
- Leave one out:  
do not use translation rules originally collected from current sentence pair
- Related to jackknife
  - 90% of training data used for rule collection
  - 10% to validate rules
  - rotate

# Translate Almost All Sentences

- Relaxed leave-one-out
  - allow rules originally collected from current sentence pair
  - very costly → only used, if everything else fails
- Allow single word translations (avoid OOV)
- Larger distortion limit
- Word deletion and insertion (very costly)

# Model Re-Estimation

- Generate 100-best list
- Collect fractional counts from derivations

⇒ Much smaller model

⇒ Sometimes better model

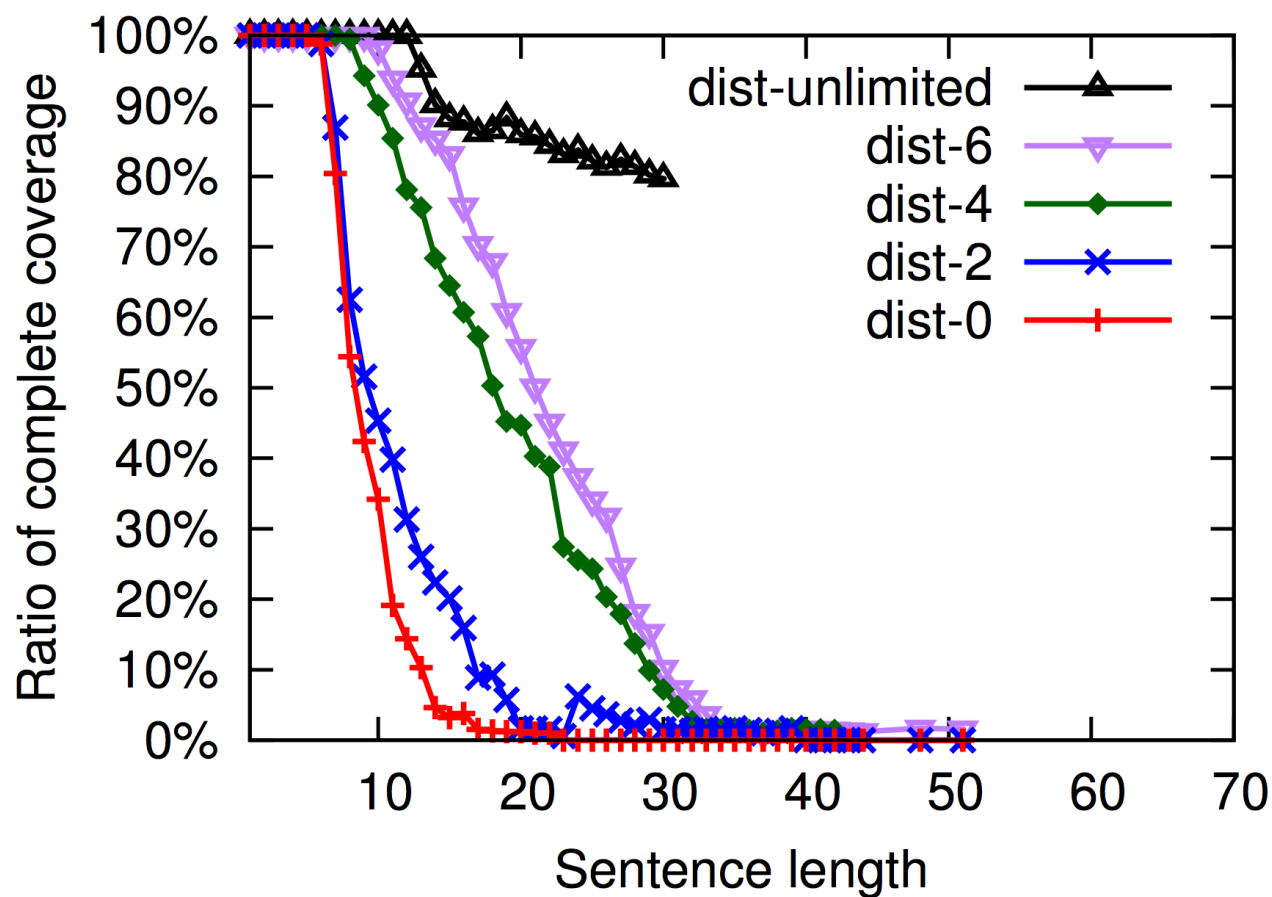
# max-violation perceptron and forced decoding

# Perceptron over Full Training Corpus



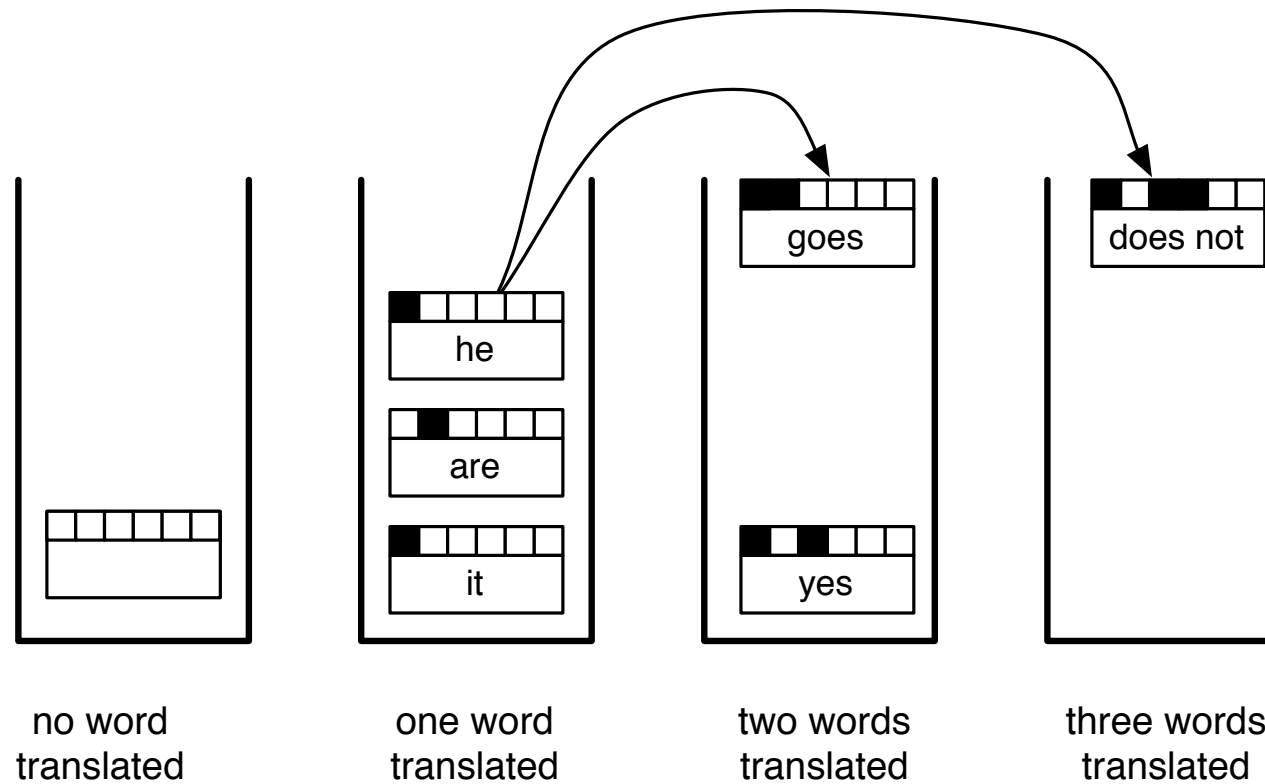
- Early work on stochastic gradient descent over full training corpus unsuccessful
- One reason: Search errors break theoretical properties of convergence
- Are unreachable reference translations a problem?
  - yes: ignoring them leaves out large amounts of training data
  - no: data selection, non-literal translations are lower quality
- Idea: update when partial reference derivation falls out of beam

# Reachability



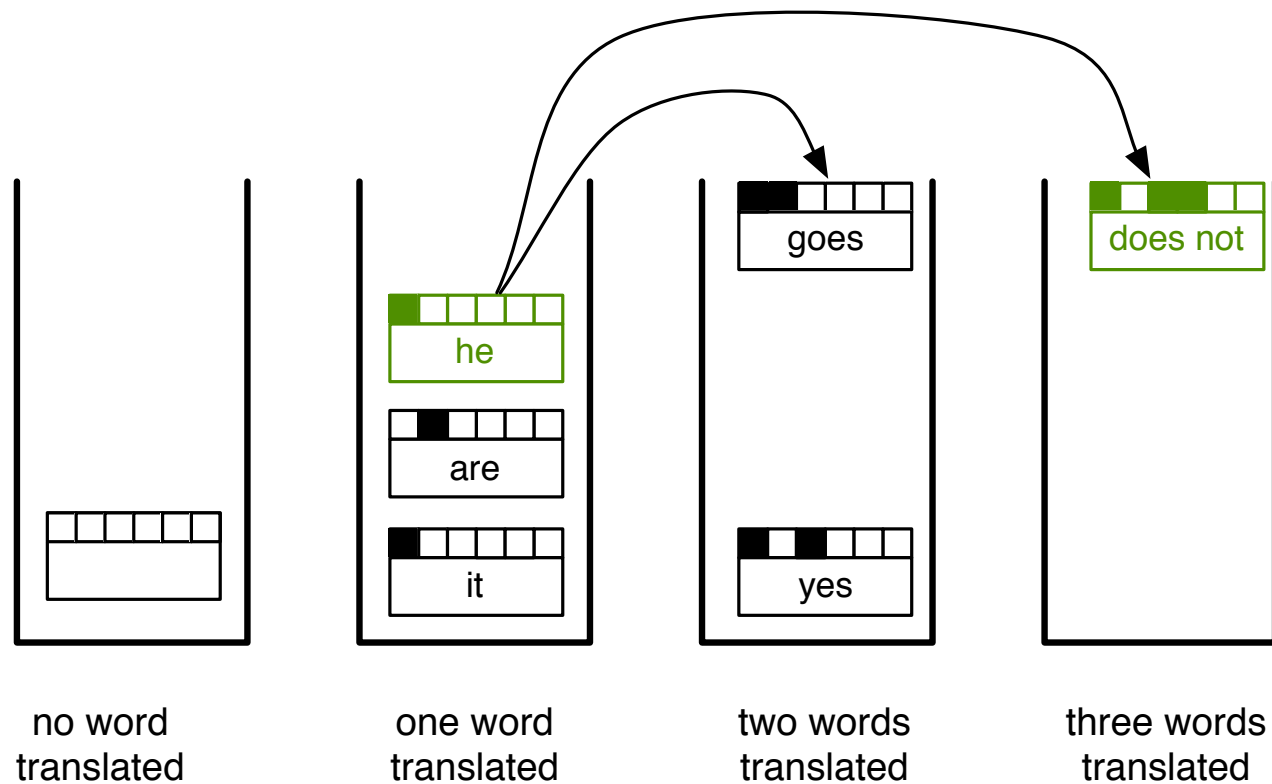
Reachability by distortion limit and sentence length  
Chinese–English NIST [Yu et al., 2013]

# Recall: Decoding



- Extend partial translations (=hypotheses) by adding translation options
- Organize hypotheses in stacks, prune out bad ones

# Matching the Reference

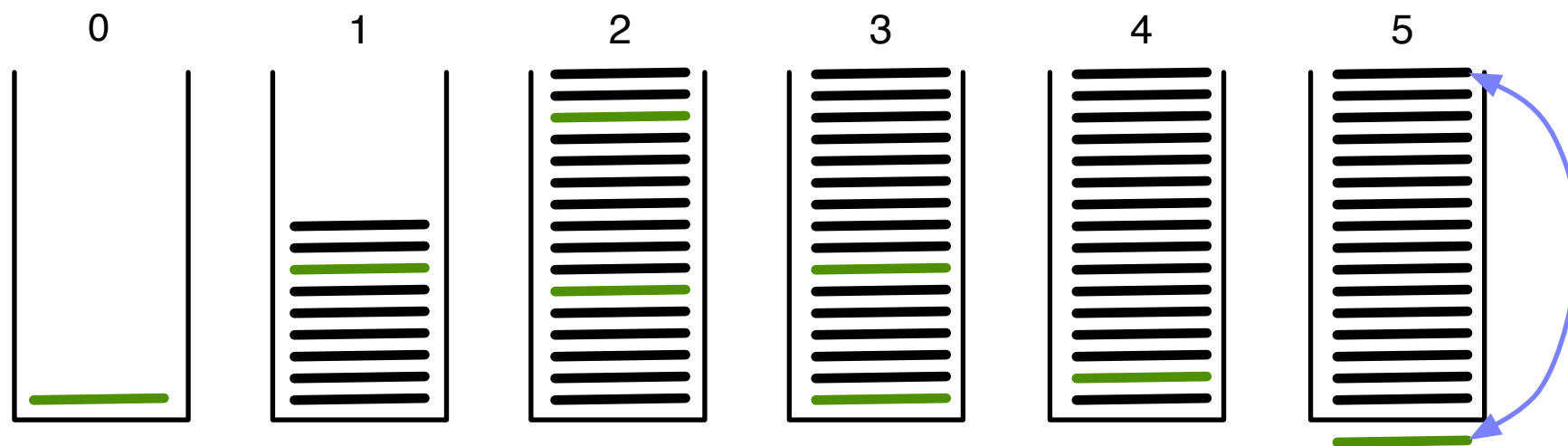


- Some hypotheses match the reference translation

he does not go home

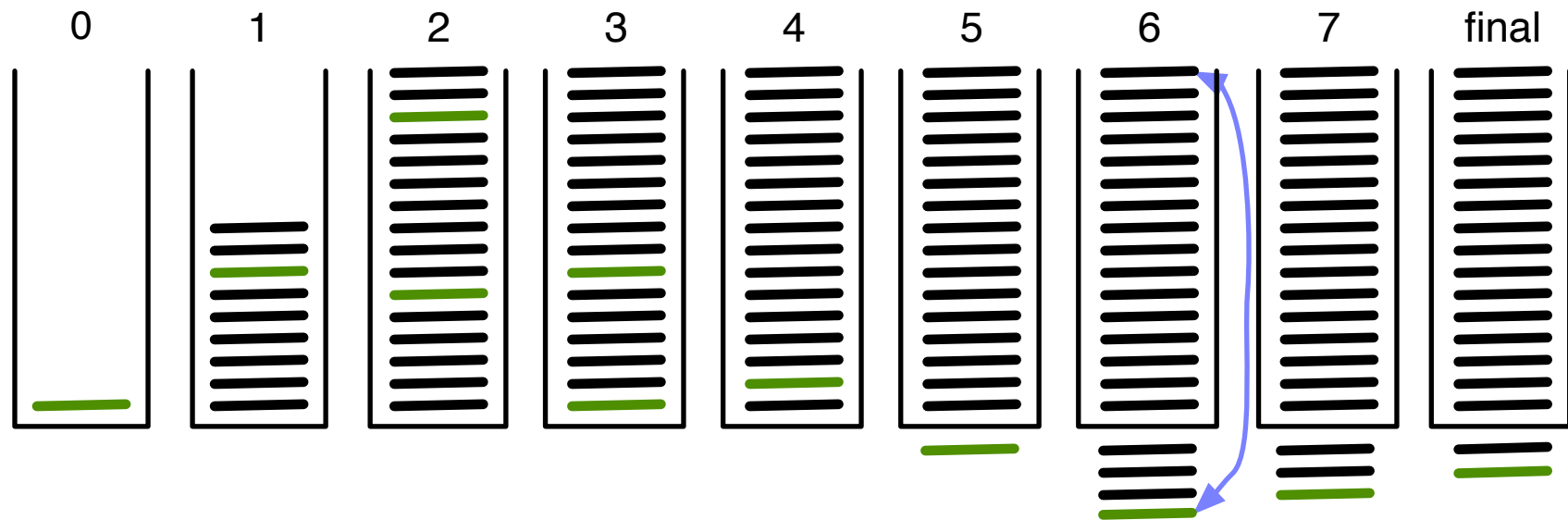


# Early Updating



- At some point the best reference derivation may fall outside the beam
- Early updating
  - perceptron update between partial derivations
  - best derivation vs. best reference derivation outside beam
- Note: a reference derivation may skip a bin (multi-word phrase translation)
  - only stop when no hope that reference derivation will be in a future stack

# Max Violation



- Complete search process
- Keep best reference derivations
- Maximum violation update
  - find stack where maximal model score difference between
    - \* best derivation
    - \* best reference derivation
  - update between those two derivations

- Shown to be successful [Yu et al., 2013]
  - optimization over full training corpus
  - over 20 million features
  - relatively small data conditions (5-9 millions words)
  - gain: +2 BLEU points
- Features
  - rule id
  - word edge features (first and last word of phrase), defined over words, word clusters, or POS tags
  - combinations of word edge features
  - non-local features: ids of consecutive rules, rule id + last two English words
- Address overfitting: leave-one-out or singleton pruning

# Summary

